

# KESTEVEN AND SLEAFORD HIGH SCHOOL

## Mathematics Scheme of Learning

### Year 9 – Term 6/Circle theorems/Surds/Ratio/Transformations

#### Intent – Rationale

A transition term before students embark on Higher GCSE maths. They have shown they are ready and key knowledge is recalled and reinforced for confidence in application at GCSE.

Sequencing – what prior learning does this topic build upon?	Sequencing – what subsequent learning does this topic feed into?
<ul style="list-style-type: none"> <li>Year 9 Term 2 angles in parallel lines and polygons</li> <li>Year 9 Term 3 index notation, Term 4 Pythagoras</li> <li>Year 8 Term 5 ratio (HSL)</li> <li>Year 8 Term 6 transformations (HSL transformation not covered full HSL only translation and simple enlargement)</li> </ul>	<ul style="list-style-type: none"> <li>GCSE circle theorem proofs, further theorems</li> <li>GCSE surd calculation, exact answers</li> <li>GCSE proportion problems</li> <li>GCSE geometrical (and graph) transformations</li> </ul>
What are the links with other subjects in the curriculum?	What are the links to SMSC, British Values and Careers?
<p>Art</p> <ul style="list-style-type: none"> <li>Mathematical ideas of pattern and shape</li> <li>Transformation/tessellation of shapes (Escher)</li> </ul> <p>Design and Technology</p> <ul style="list-style-type: none"> <li>Ratio calculations</li> <li>Construction and transformations strands of shape, space and measures</li> </ul> <p>Science</p> <ul style="list-style-type: none"> <li>Indices and exact measurements</li> <li>Ratio problems</li> </ul>	<ul style="list-style-type: none"> <li>GB4efghi</li> </ul>
What are the opportunities for developing literacy skills and developing learner confidence and enjoyment in reading?	What are the opportunities for developing mathematical skills?

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- 'The Math Book' - Clifford Pickover
- 'Alex's Adventures in Numberland' – Alex Bollos

- New language used in circle theorems
- Working with exact answers
- Using combined knowledge to solve ratio problems including fractions and percentages

## **Mathematics Scheme of Learning** **Year 9 – Term 6**

### **Intent – Concepts**

#### **What knowledge will students gain and what skills will they develop as a consequence of this topic?**

##### **National Curriculum 2014 Programme of Study Reference**

Find the area and circumference of a circle, area and perimeter of a sector, identify all parts of a circle (radius, diameter, circumference, sector, arc, segment, tangent to). Find missing angles on parallel lines using all known rules (alternate, corresponding, co-interior)

Able to confidently work with fractions and decimals, understand the difference of two squares and simple binomial expansions, able to use Pythagoras' Theorem with ease

Extend and formalise knowledge of ratio and proportion in working with measures and geometry, and in formulating relations algebraically, use ratio notation including reduction to simplest form, divide a quantity into two parts in a given part:part or part:whole ratio, express the division of a quantity into two parts as a ratio, understand that a multiplicative relationship between two quantities can be expressed as a ratio or a fraction

Identify properties of, and describe the results of, translations, rotations, reflections and enlargements applied to given figures

##### **Know**

Know the parts of a circle. Recognise radii isosceles triangles, tangent right angled triangles, cyclic quadrilaterals. Use basic circle theorems to find missing angles.

Simplify surds and surd expressions.

Recap simplifying ratios and dividing in a ratio. Combining ratios.

##### **Apply**

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<p>Give reasonings to angles found Simplify surd ratios Ratio worded problems <b>Extend</b> Compound circle theorems Expanding double bracket surd expressions. Changing ratios</p>	
What subject specific language will be used and developed in this topic?	What opportunities are available for assessing the progress of students?
<p>Circle, semi-circle, circumference, radius, radii, tangent, diameter, segment, arc, sector, chord, subtended, cyclic quadrilateral, isosceles, right angled, equal, perpendicular. Surd, irrational, expression, square number, factor, coefficient. Ratio, express, divide, proportion, fraction</p>	<ul style="list-style-type: none"> <li>• End of term test prior to transformations – GCSE setting</li> <li>• Mid Term marking targets</li> <li>• Common misconceptions:</li> <li>• Students confusing radius and diameter, not recognising isosceles or right-angled triangles. Students incorrectly using a cyclic quadrilateral theorem when not all vertices lie on the circumference.</li> <li>• Students finding the square number factor but incorrectly simplify to get coefficient of surd.</li> <li>• Students confusing dividing in a ratio questions with using one quantity to find another. Students not expressing a ratio in its simplest form. Students incorrectly rearranging expressing ratios using equivalent fractions.</li> </ul>

Circle Theorems	R	A	G
Know the parts of a circle			
Recognise isosceles and right-angled triangles in circles			
Recognise cyclic quadrilaterals in circles			
Use basic circle theorems to find missing angles			

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Surds	R	A	G
Know the definition of a surd			
Simplify a surd			
Simplify surd expressions			
Add/Subtract surds			

Ratio	R	A	G
Create and simplify ratios			
Divide an amount in a given ratio			
Solve ratio problems when an amount is known			
Expressing variables in a ratio			
Challenge: Changing ratios			

## Intent – Concepts

Lesson title	Learning challenge	Higher level challenge	Suggested activities and resources
France Trip non-attendees Activity			
Circle Theorems	Know the parts of a circle. Recognise isosceles triangles in circles		Starter: label parts of a circle Finding angles in radii isosceles triangles. <i>Angle at centre twice angle at circumference</i> Problems linking to radii isosceles triangles <i>Angles in same segment are equal</i> <i>Radius meets tangent at 90°</i>

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			Right angled triangle problems – link to Pythagoras too. NB Y9 Circle Theorems PPT
	Recognise cyclic quadrilaterals in circles		<i>Opposite angles in a cyclic quadrilateral sum to <math>180^\circ</math> or are supplementary.</i> <i>The angle subtended in a diameter of a circle is <math>90^\circ</math></i>
	Use basic circle theorems to find missing angles		Mixed problems – HRE multiple choice reasoning PP
Surd	Know the definition of a surd. Simplify a surd		NB Y9 Surds PPT Starter: finding square number factors. Simplify eg $\sqrt{50}$
	Simplify surd expressions	Coefficients of surds eg $2\sqrt{50} \times 3\sqrt{8}$ Double brackets	$\sqrt{50} \times \sqrt{8}$ $\sqrt{150} / \sqrt{5}$ $2(\sqrt{20} + 5)$
	Add/Subtract surds		Refer to rules of adding letters
Ratio	Create and simplify ratios. Divide an amount in a given ratio	<a href="#">Ratio with surds</a>	NB Y9 Ratio PPT
	Solve ratio problems when an amount is known	Worded problems	<a href="#">Ratio card sort</a>
	Expressing variables in a ratio		x:y express x in terms of y
	Combining ratios		a:b b:c find a:c <a href="#">Mixed worksheet (GCSE &amp; JMC)</a>
	Challenge: Changing ratios		
Baseline Test for GCSE setting			

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Transformations	Translation		Draw and describe NB Y9 Transformations PPT
	Reflection	Identifying variant points	Draw and describe, recap equation of straight line
	Rotation	Identifying variant points	Draw and describe, centres not always (0,0)
	Enlargement	Negative fractional scale factor	Draw and describe, including fractional scale factors.
	Combined Transformations		